Introduction to Quantum computing and superconducting qubits

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@Special topics of nano physics and emergent quantum matters

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Quantum technology: the second quantum revolution

By Jonathan P. Dowling 1 and Gerard J. Milburn 2

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We are currently in the midst of a second quantum revolution. The first quantum revolution gave us new rules that govern physical reality. The second quantum revolution will take these rules and use them to develop new technologies. In this review we discuss the principles upon which quantum technology is based and the tools required to develop it. We discuss a number of examples of research programs that could deliver quantum technologies in coming decades including: quantum information technology, quantum electromechanical systems, coherent quantum electronics, quantum optics and coherent matter technology.

Keywords: quantum technology; quantum information; nanotechnology, quantum optics, mesoscopics; atom optics



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What are the new technologies that can be developed from quantum mechanics?

Different facets of quantum Technologies

"European Quantum Technologies Flagship Programme"

- Quantum computation
- Quantum simulation
- Quantum communication
- Quantum sensing and metrology





(https://ec.europa.eu/digital-single-market/en/quantum-technologies)

Different facets of quantum Technologies

"European Quantum Technologies Flagship Programme"

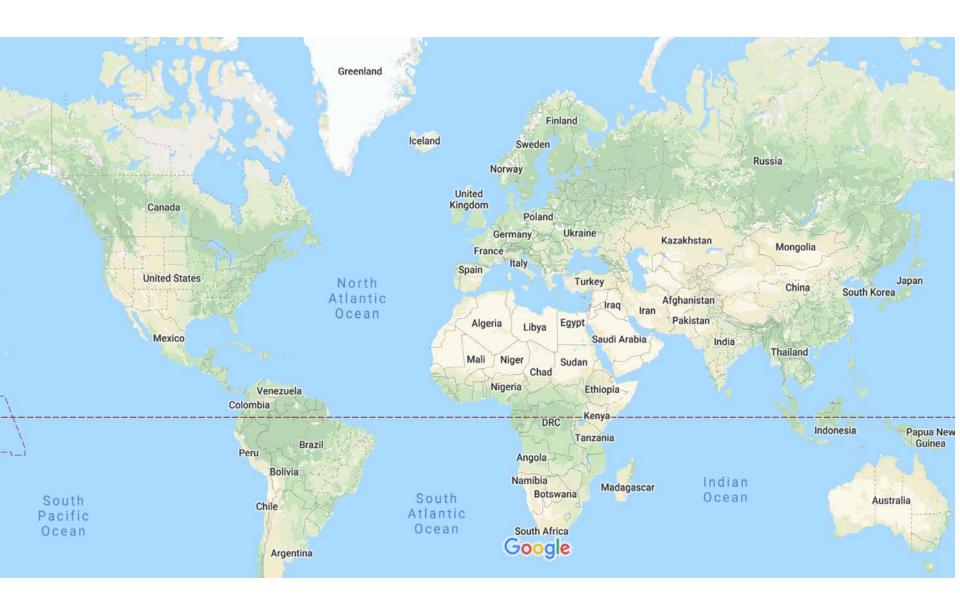
- Quantum computation
- Quantum simulation
- Quantum communication

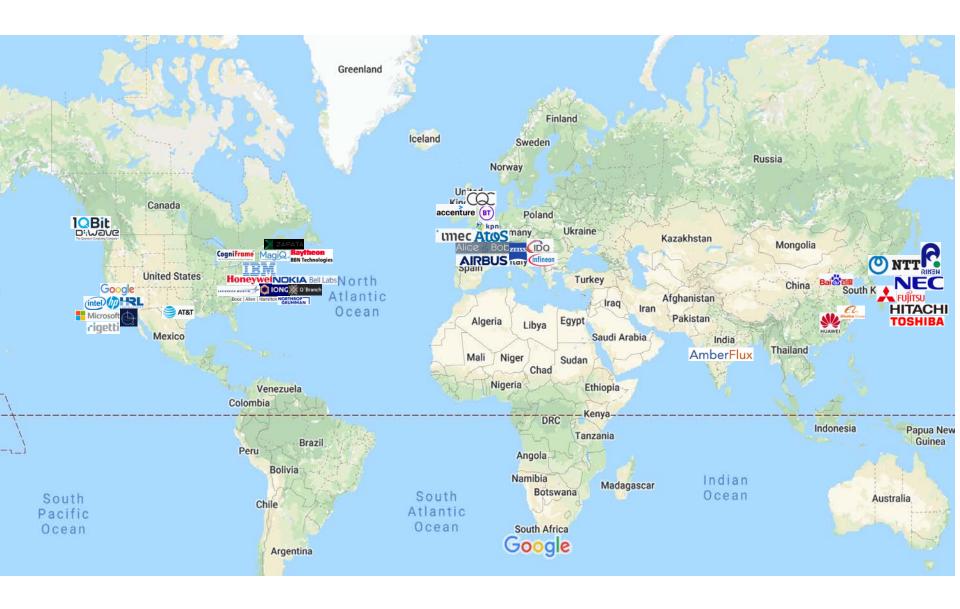


Quantum sensing and metrology



(https://ec.europa.eu/digital-single-market/en/quantum-technologies)



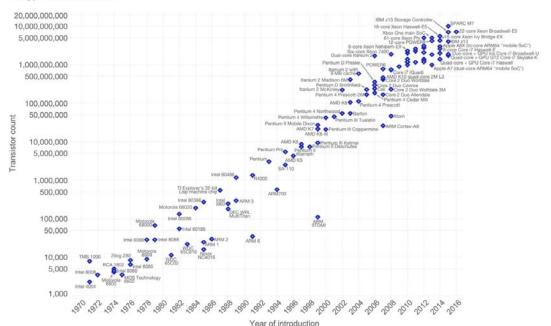


What's wrong with classical computer?

Moore's Law: the <u>number of transistors</u> in a dense integrated circuit <u>doubles</u> about every two years.

Moore's Law – The number of transistors on integrated circuit chips (1971-2016) Our World

Moore's law describes the empirical regularity that the number of transistors on integrated circuits doubles approximately every two years. This advancement is important as other aspects of technological progress – such as processing speed or the price of electronic products – are strongly linked to Moore's law.

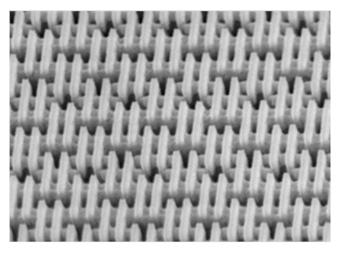




Gordon Moore in 2004

Limitation of of Moore's Law

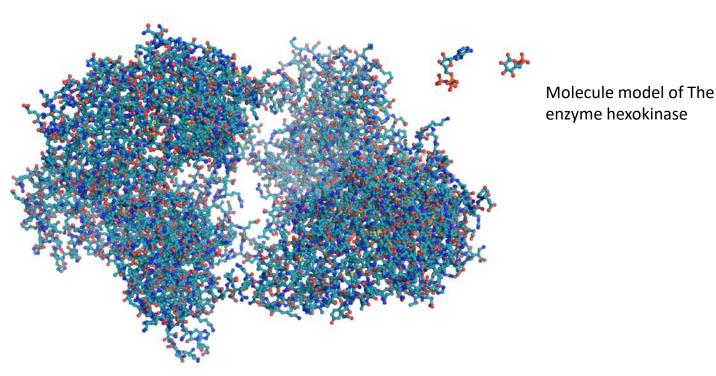
- Difficulty of fabrication
- Heat dissipation problem of nano-structures
- Quantum effects of nano-devices.



7nm MOSFETs by TSMC

https://www.tsmc.com/english/dedicatedFoundry/technology/logic.htm#l_7nm_technology

Difficulty of simulating quantum system

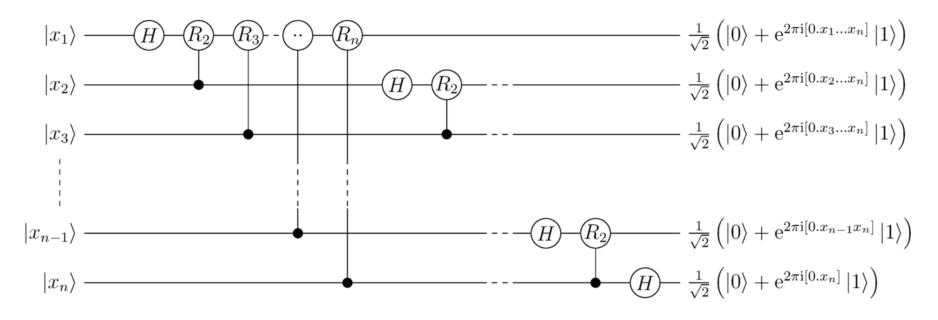


https://en.wikipedia.org/wiki/Protein

More efficient Method to Solve Problem

 We develop new methods to solve problem more efficiently.

Quantum Fourier transform quantum circuit



What are quantum computers?

Question

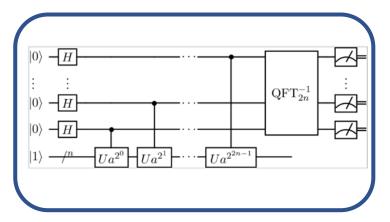
Quantum computers:

Devices can store and process information according to the principles of quantum mechanics

Gate-based Quantum Computer

- Universal quantum computer.
- The processing of a task is based on a series of unitary transformation of quantum states.
- Commonly use circuit model to describe process.
- Comparable to quantum algorithm development

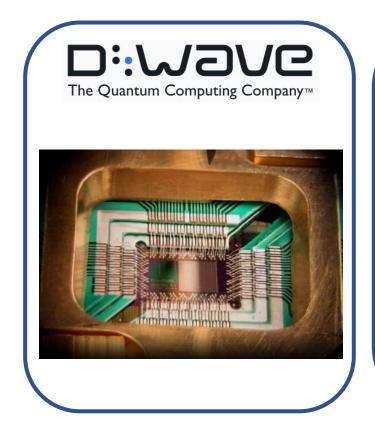


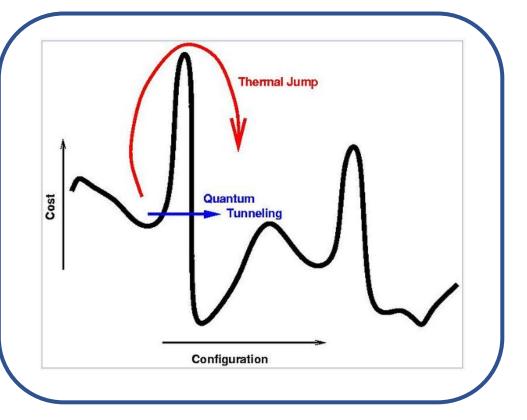


https://en.wikipedia.org/wiki/Shor%27s_algorithm

Quantum Annealer

- Cannot execute quantum circuit.
- Quantum optimization.

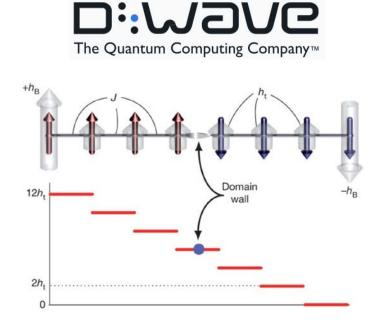




Quantum Simulator

- Construct controllable quantum sub-system to simulate real quantum system
- First Proposal: Feynman, Richard (1982). "Simulating Physics with Computers"





M. W. Johnson et al., *Nature* **473**, 194(2011)

Other Type of Quantum Processor

• 九章量子電腦: Special for Gaussian boson sampling



Type of Quantum Computer

- Gate-based Quantum Computer
- Quantum Annealer(Quantum optimization)
- Quantum Simulator
- Special Task Quantum processor

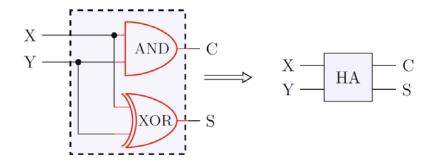
What's the difference between classical computer and quantum computer?

Circuit Model of Computation

Three main elements of circuit model:

- 1. A set of values.
- 2. A set of gate labels.
- 3. A labelled directed acyclic graph.

Example: The half adder(classical computation)



| X | Y | $S(X \oplus Y)$ | С |
|---|---|-----------------|---|
| 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 1 |

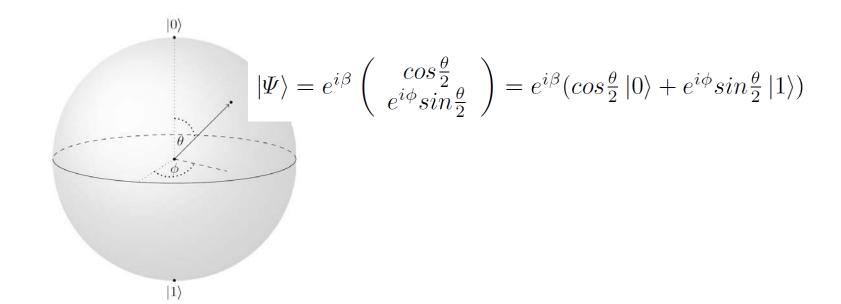
Concept of Classical vs Quantum Computing

| | Classical Computing | Quantum Computing |
|-------------|---------------------|---|
| Memory Unit | Bit -> Byte | $ 0\rangle 1\rangle \rightarrow \Psi\rangle$ |
| Write in | Initialize bytes | Initialize $ \Psi angle$ |
| Computation | Logic gate | Apply Operators $\mathbf{X} \equiv \Phi angle\langle\Psi $ |
| Read out | Read bytes | Measure $ \Psi angle$ (Born's rule) |

Single Quantum Bit(Qubit)

Qubit: Information stored in $|\Psi\rangle = c_1|0\rangle + c_2|1\rangle$ $|c_1|^2 + |c_2|^2 = 1$

Frequently use Bloch sphere representing $|\Psi\rangle$



Commonly Used Single Qubit Gate

Pauli-X (X)
$$-\mathbf{X}$$
 $-\mathbf{G}$ $\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$
Pauli-Y (Y) $-\mathbf{Y}$ $\begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}$
Pauli-Z (Z) $-\mathbf{Z}$ $\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$
Hadamard(H) $-\mathbf{H}$ $-\mathbf{G}$ $\begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix}$
Phase (S) $-\mathbf{G}$ $\begin{pmatrix} 1 & 0 \\ 0 & i \end{pmatrix}$
 $\pi/8$ (T) $-\mathbf{T}$ $\begin{pmatrix} 1 & 0 \\ 0 & e^{i\pi/4} \end{pmatrix}$

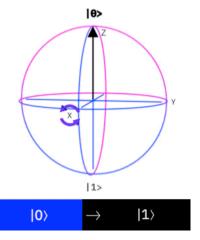
Pauli X(X) gate

$$|0\rangle$$
 $|1\rangle$

$$\sigma_X |0\rangle \Rightarrow \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \\ 1 \end{pmatrix} \Rightarrow |1\rangle$$

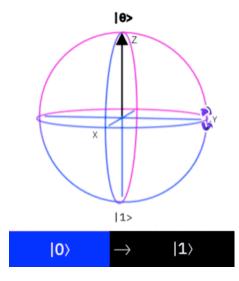
$$|1\rangle$$
 $|0\rangle$

$$\sigma_X|1\rangle = |0\rangle$$

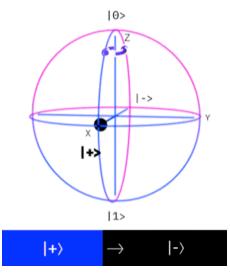


Pauli Y(Y) and Pauli Z(Z) gate

$$\sigma_Y \equiv \begin{pmatrix} 0 - i \\ i & 0 \end{pmatrix}$$



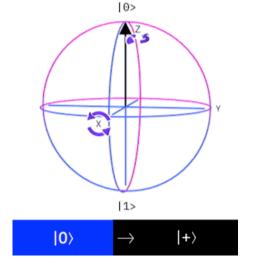
$$\sigma_Z \equiv \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$



https://quantum-computing.ibm.com/docs/circ-comp/q-gates

Hardama Gate

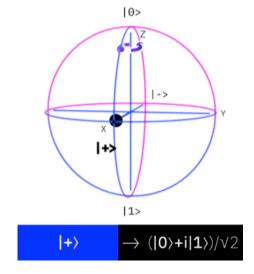
$$\mathbf{H} \equiv \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix}$$



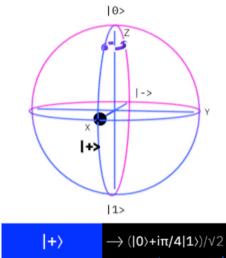
Generate superposition states of $|0\rangle |1\rangle$

S and T Gate

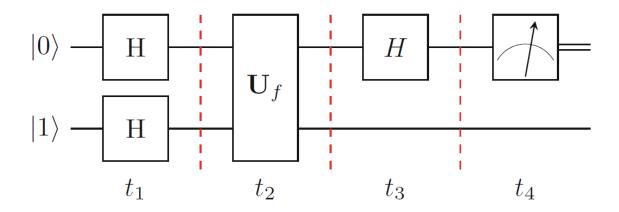
Phase (S)
$$\begin{pmatrix} 1 & 0 \\ 0 & i \end{pmatrix}$$

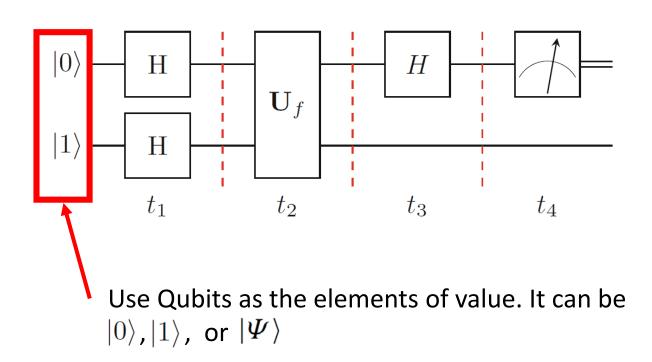


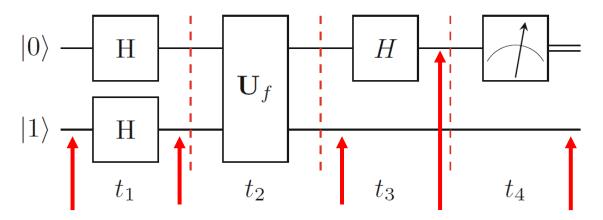
$$\pi/8$$
 (T) $\begin{pmatrix} 1 & 0 \\ 0 & e^{i\pi/4} \end{pmatrix}$



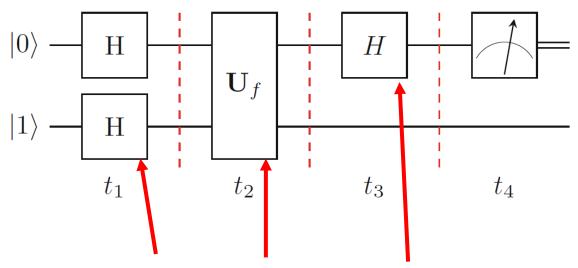
https://quantum-computing.ibm.com/docs/circ-comp/q-gates



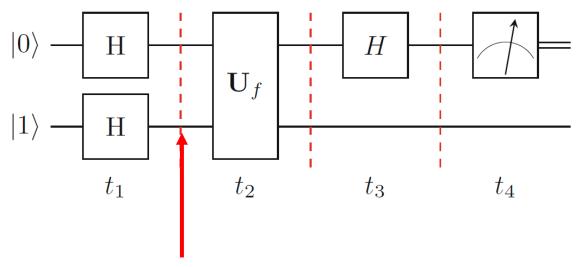




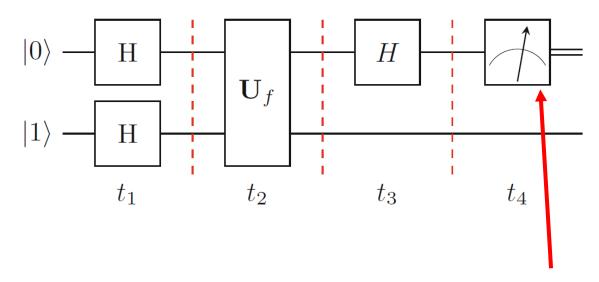
Each single wire represents a qubit ket. The convention time is assumed to run from left to right in the diagram. The state is not altered until the wire enters a quantum gate or a measurement device.



The quantum gates that represent operations to the qubit kets.



The output qubit kets of previous gate become the input of the next gate.



A measurement to readout the ket

Can we construct a quantum algorithm that works better than classical algorithm?

Can we construct a quantum algorithm that works better than classical algorithm?

Deutsch's algorithm(1985): The first quantum algorithm outperformed classical algorithm.

Binary function f(x)

Consider a binary function f(x): only four possibilities

| Input | A | В | С | D |
|-------|---|---|---|---|
| 0 | 0 | 0 | 1 | 1 |
| 1 | 0 | 1 | 0 | 1 |

Binary function f(x)

The output is independent of input: constant function(Case A and D)

The output depends on input: balanced function(Case B and C)

| Input | A | В | С | D |
|-------|---|---|---|---|
| 0 | 0 | 0 | 1 | 1 |
| 1 | 0 | 1 | 0 | 1 |

Deutsch's Problem

Give a binary function f(x), is f(x) a constant function of balanced function?

Deutsch's Problem

Give a binary function f(x), is f(x) a constant function of balanced function?

Constant: f(0) = f(1)

 $\mathsf{Balanced}(f(0)) = \widetilde{f}(1)$

Classical Algorithm

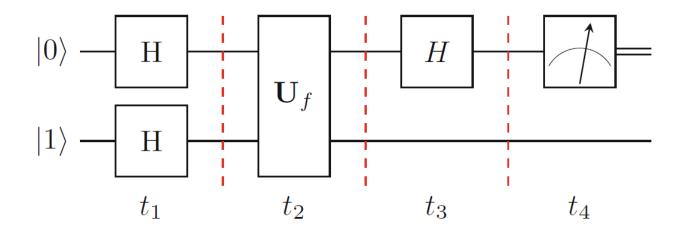
Plug in 0 and 1. Find out f(0)=? and f(1)=? Then, one can determine f(x) is a constant or a balanced function.

At least two evaluations to find out f(0) and f(1)

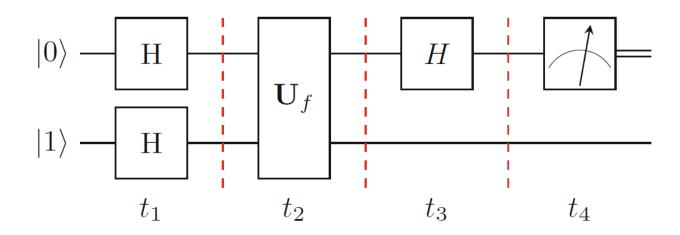
Quantum Algorithm

Allow you to only evaluate f(x) once!

How?



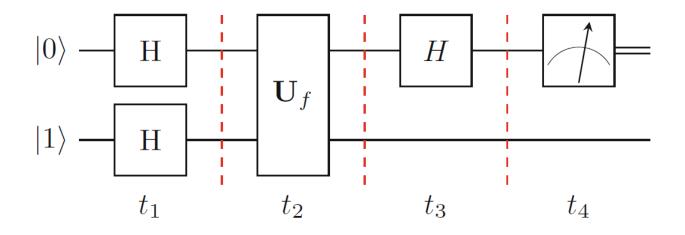
Let's look results after each gate First initialized two qubits to be $|0\rangle$ and $|1\rangle$



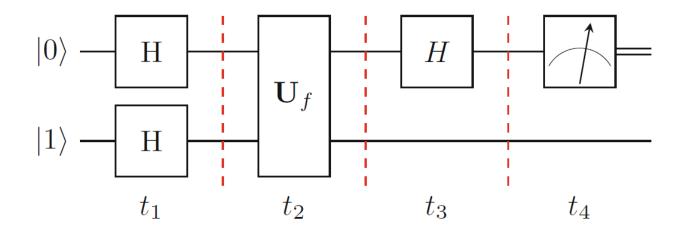
Operation of two Hadamard gates

$$\mathbf{H}|0\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle)$$

$$\mathbf{H} |1\rangle = \frac{1}{\sqrt{2}} (|0\rangle - |1\rangle)$$

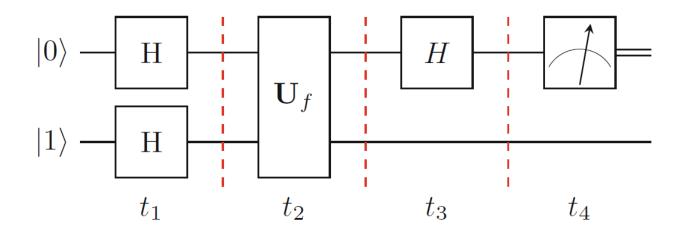


After t1
$$|\psi(t_1)\rangle = \frac{1}{2}\Big((|0\rangle + |1\rangle)\otimes(|0\rangle - |1\rangle)\Big) = \frac{1}{2}\Big(|00\rangle + |10\rangle - |01\rangle - |11\rangle\Big)$$



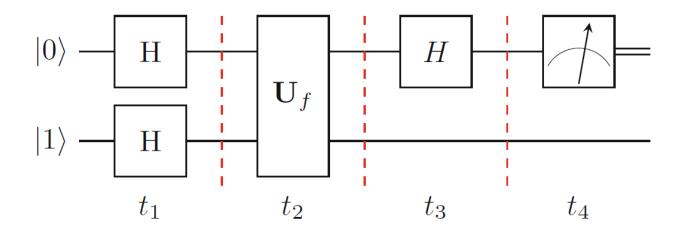
After t1
$$|\psi(t_1)\rangle = \frac{1}{2}\Big((|0\rangle + |1\rangle) \otimes (|0\rangle - |1\rangle)\Big) = \frac{1}{2}\Big(|00\rangle + |10\rangle - |01\rangle - |11\rangle\Big)$$

A superposition states contained all possible combinations!

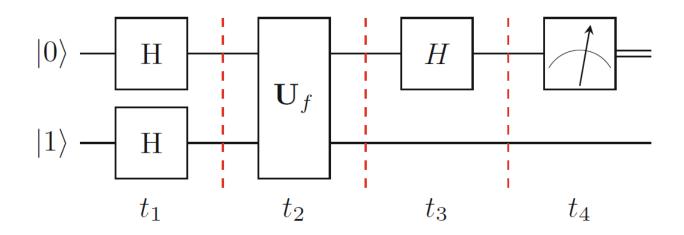


After t1
$$|\psi(t_1)\rangle = \frac{1}{2}\Big((|0\rangle + |1\rangle) \otimes (|0\rangle - |1\rangle)\Big) = \frac{1}{2}\Big(|00\rangle + |10\rangle - |01\rangle - |11\rangle\Big)$$

Quantum Parallelism

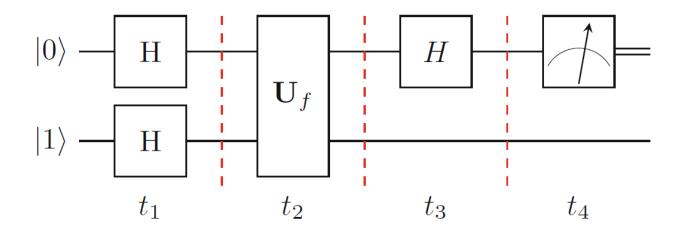


After t2:
$$|\psi(t_2)\rangle = \frac{1}{2} \Big(|0\rangle \otimes |f(0)\rangle + |1\rangle \otimes |f(1)\rangle - |0\rangle \otimes |f(0) \oplus 1\rangle - |1\rangle \otimes |f(1) \oplus 1\rangle \Big)$$



After t3: Constant:
$$f(0) = f(1)$$
 $|\psi(t_3)\rangle = \frac{1}{\sqrt{2}}(|0\rangle) \otimes (|f(0)\rangle - |\widetilde{f}(0)\rangle)$ $|\psi(t_3)\rangle = \frac{1}{\sqrt{2}}(|1\rangle) \otimes (|f(0)\rangle - |\widetilde{f}(0)\rangle)$

Quantum Interference



After t4:

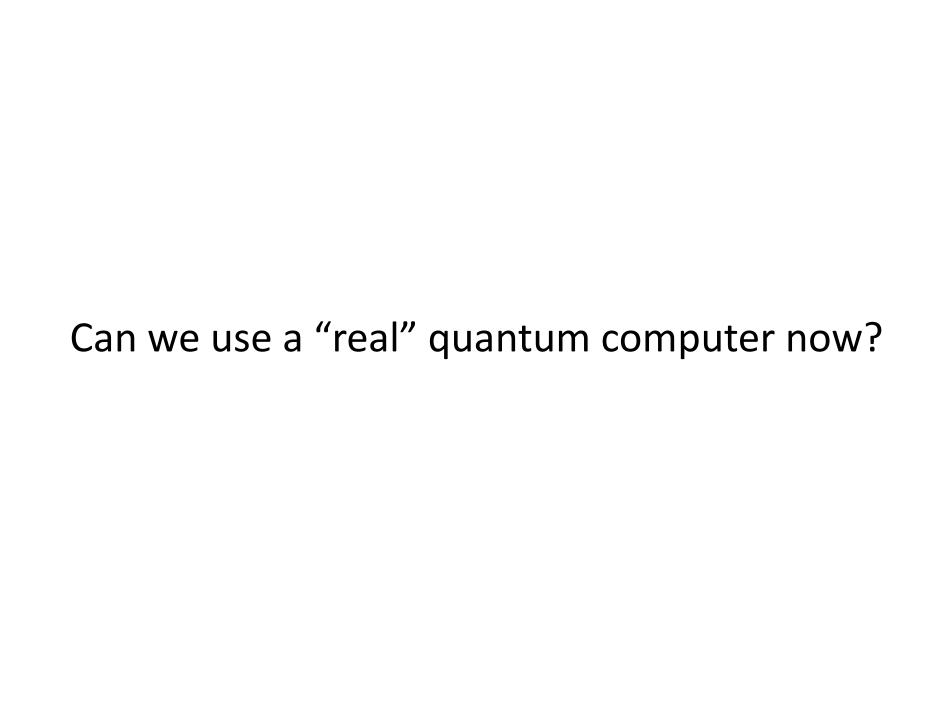
Constant: get 0

Balanced: get 1

Only evaluate f(x) once in $U_f!$

Key Elements of Advantage in Quantum Information

- Superposition + Quantum interference
- Entangle States

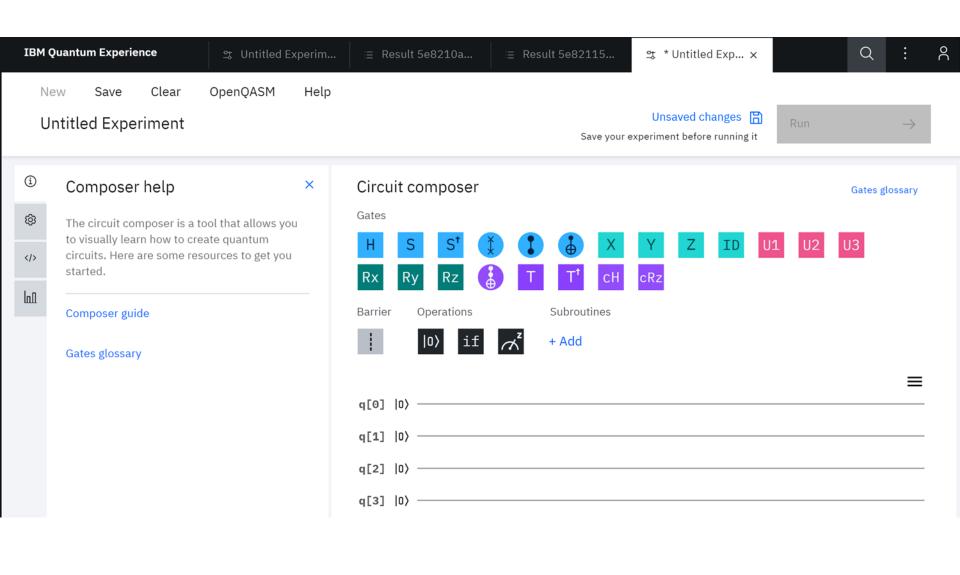


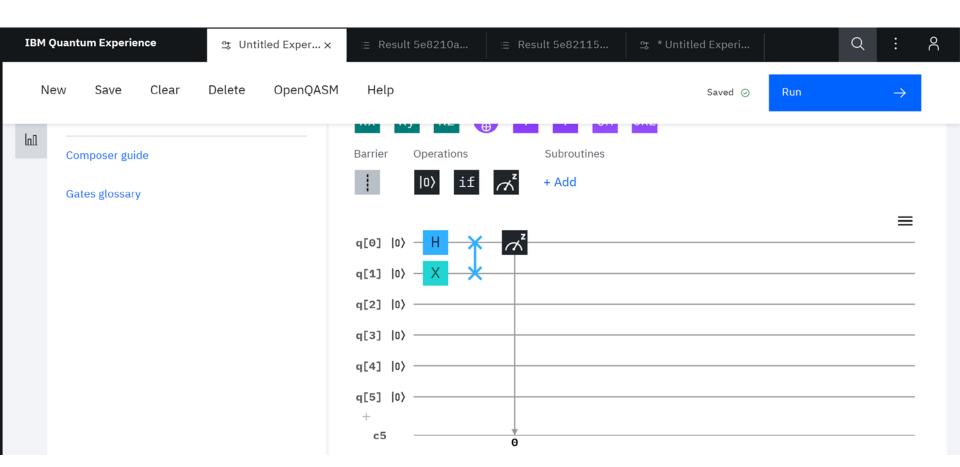
Can we use a "real" quantum computer now?

YES!!!

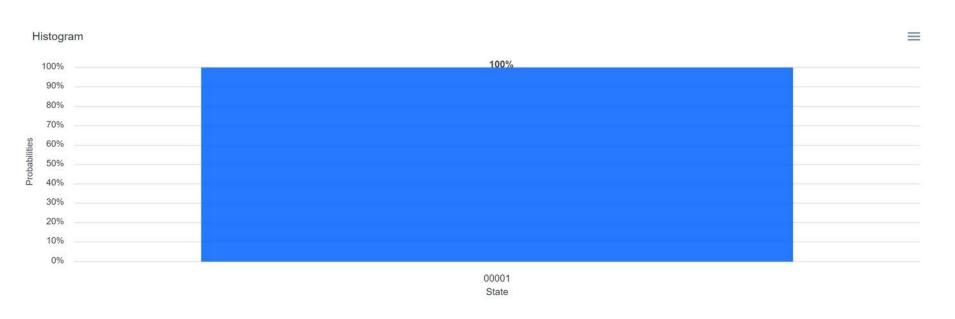
IBM Quantum Experience

- https://quantum-computing.ibm.com/
- You can construct your own quantum circuit online.
- Send your quantum circuit to a simulator or a real IBM quantum computer to run!

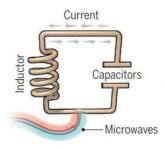




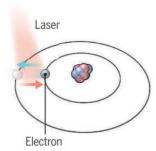
Result of simulation(1024 times of measurements)



What are the possible quantum systems can be made to be quantum computer?



Superconducting loops



Trapped ions

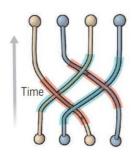
A resistance-free current oscillates back and forth around a circuit loop. An injected microwave signal excites the current into superposition states.

Electrically charged atoms, or ions, have quantum energies that depend on the location of electrons. Tuned lasers cool and trap the ions, and put them in superposition states.



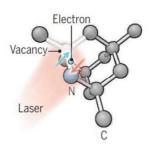
Silicon quantum dots

These "artificial atoms" are made by adding an electron to a small piece of pure silicon. Microwaves control the electron's quantum state.



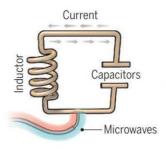
Topological qubits

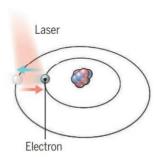
Quasiparticles can be seen in the behavior of electrons channeled through semiconductor structures. Their braided paths can encode quantum information.



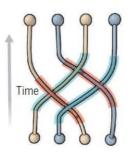
Diamond vacancies

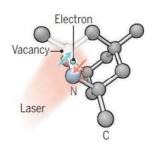
A nitrogen atom and a vacancy add an electron to a diamond lattice. Its quantum spin state, along with those of nearby carbon nuclei, can be controlled with light.











Superconducting loops

A resistance-free current oscillates back and forth around a circuit loop. An injected microwave signal excites the current into superposition states.

Longevity (seconds) 0.00005

Trapped ions

Electrically charged atoms, or ions, have quantum energies that depend on the location of electrons. Tuned lasers cool and trap the ions, and put them in superposition states.

Silicon quantum dots

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Topological qubits

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Diamond vacancies

A nitrogen atom and a vacancy add an electron to a diamond lattice. Its quantum spin state, along with those of nearby carbon nuclei, can be controlled with light.

Logic success rate

99.9%

>1000

0.03

N/A

10

99.4%

14

~99%

N/A

99.2%

Number entangled

Intel

N/A Microsoft. Bell Labs

Quantum Diamond Technologies

Company support Google, IBM, Quantum Circuits

Pros

Fast working. Build on existing semiconductor industry.

Cons

Collapse easily and must be kept cold.

Very stable. Highest achieved gate fidelities.

Slow operation. Many lasers are needed.

Stable. Build on existing semiconductor industry.

Only a few entangled. Must be kept cold.

Greatly reduce errors.

Existence not yet confirmed.

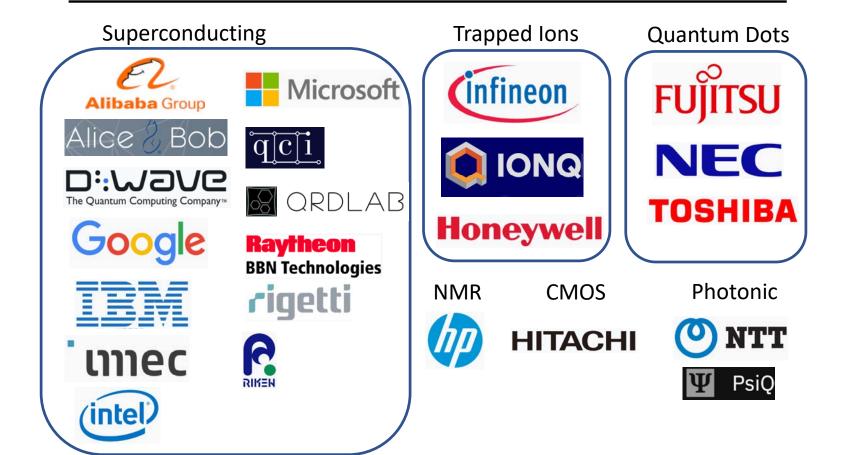
Can operate at room temperature.

Difficult to entangle.

Note: Longevity is the record coherence time for a single qubit superposition state, logic success rate is the highest reported gate fidelity for logic operations on two qubits, and number entangled is the maximum number of qubits entangled and capable of performing two-qubit operations.

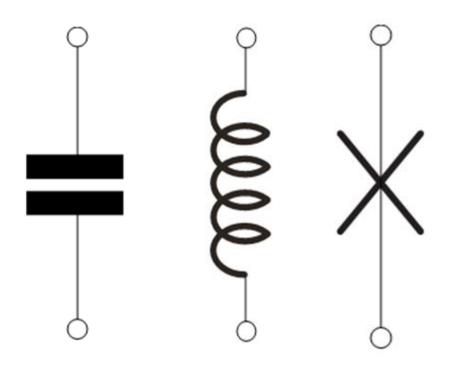
Science 02 Dec 2016: Vol. 354, Issue 6316, pp. 1090-1093 DOI: 10.1126/science.354.6316.1090

Quantum Hardware R&D!

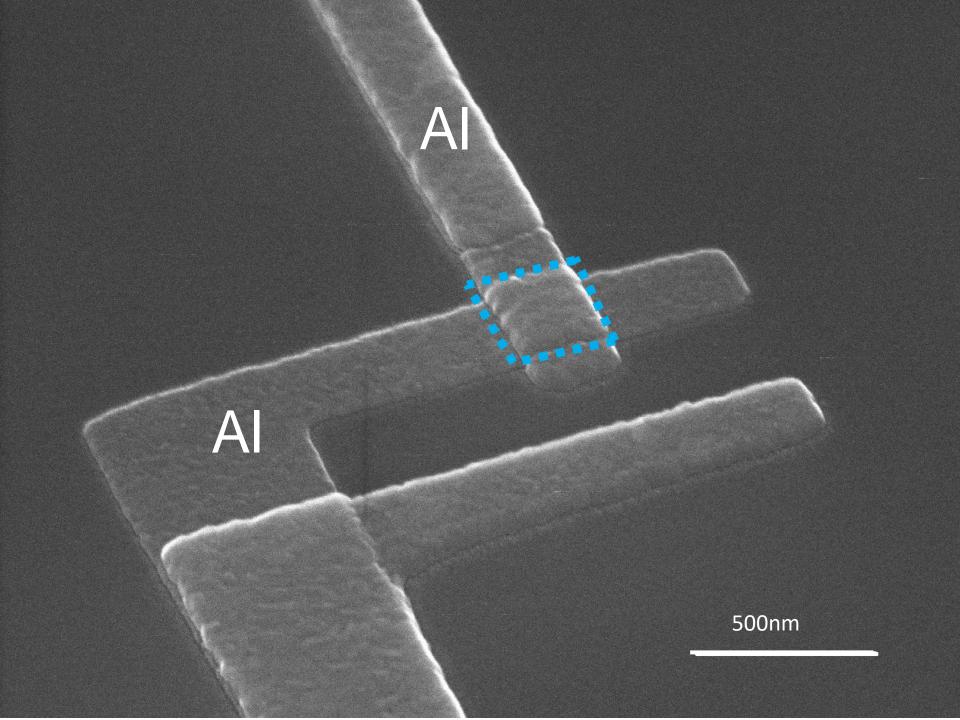


How to build a superconducting qubit?

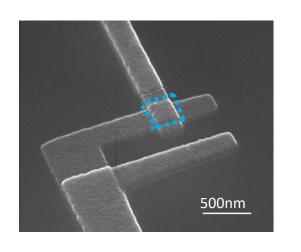
Building blocks of superconducting artificial atoms

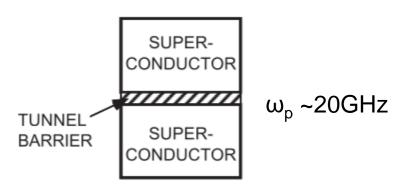


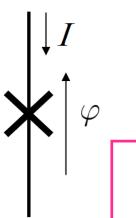
quantum (330) set



Josephson Al/AlOx/Al tunnel junction: a nonlinear dissipationless inductor





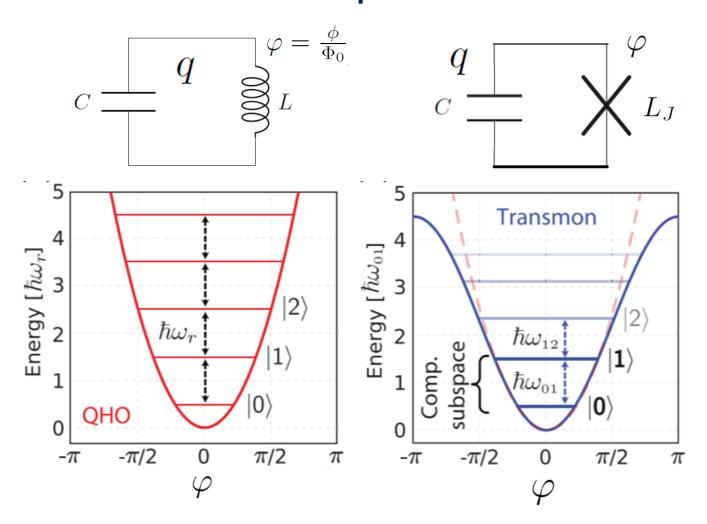


$$V = \frac{\hbar}{2e} \frac{\partial}{\partial t} \varphi$$
$$I = I_c sin\varphi$$

$$I = I_c sin\varphi$$

$$L_J(\varphi) = \frac{\phi_0}{I_c \cos \varphi} = \frac{L_J(0)}{\cos \varphi}$$
$$E(\varphi) = \frac{I_c \Phi_0}{2\pi} (1 - \cos \varphi) \equiv E_J (1 - \cos \varphi)$$

Josephson Al/AlOx/Al tunnel junction: a nonlinear dissipationless inductor

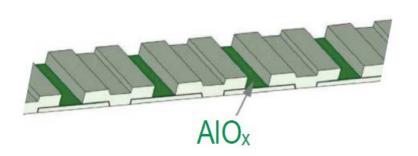


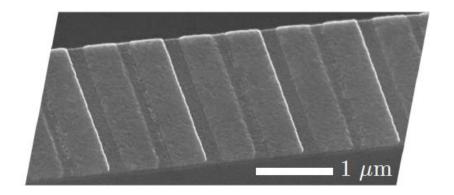
Josephson Junction Chain: Superinductor

$$L_J/\sqrt{A} > 10^4 \mu_0$$

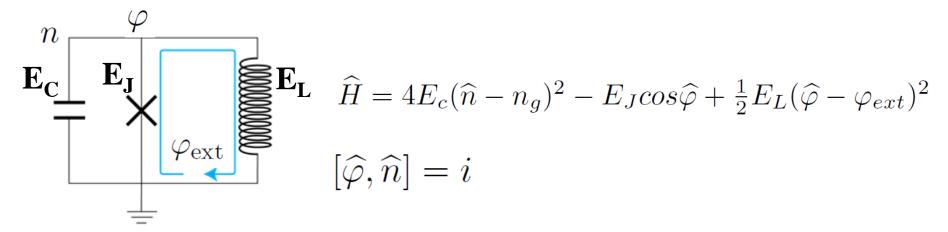
enormous (kinetic) inductance!



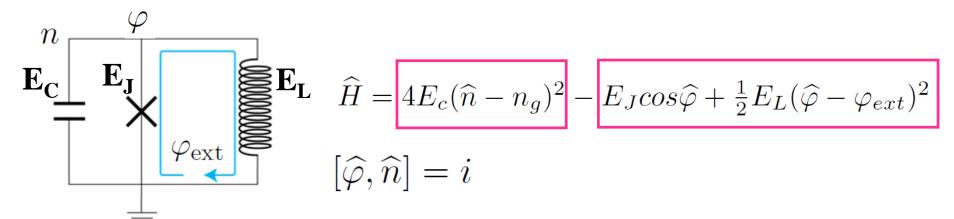




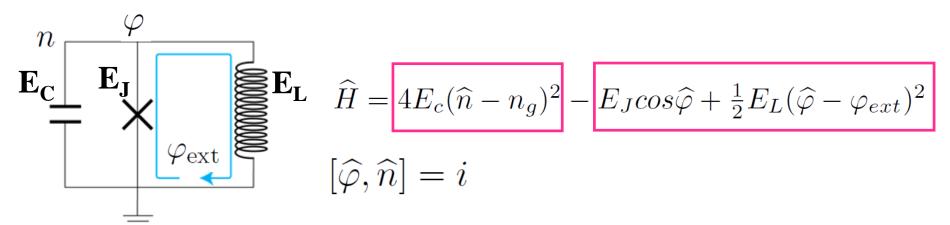
Particle in a box physics: Design box!

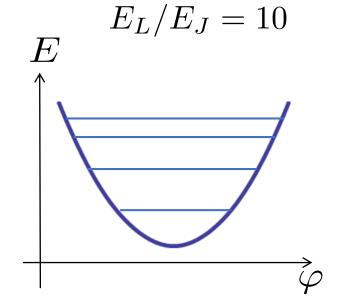


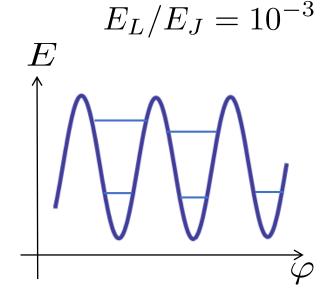
Particle in a box physics: Design box!



Particle in a box physics: Design box!

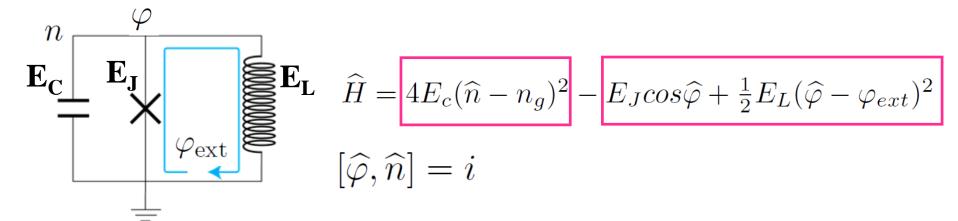




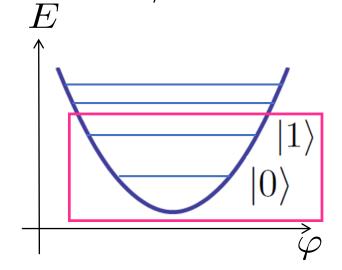


Artificial atoms: engineerable energy states and transitions

Confine Dynamics: Qubit



$$E_L/E_J = 10$$



$$|\psi\rangle = \alpha |0\rangle + \beta |1\rangle$$

Qubit: information storage within $|\psi\rangle$

Time scale of loss information: T1 and T2

$$\frac{1}{T_2} = \frac{1}{2T_1} + \frac{1}{T_{\phi}}$$

Decoherence time Relaxation time Dephasing time

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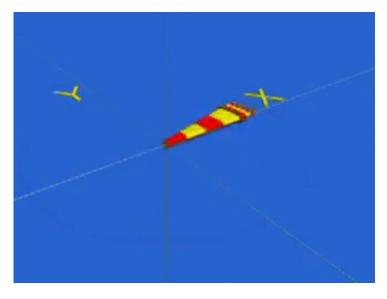
7

Relaxation

Time scale of loss information: T1 and T2

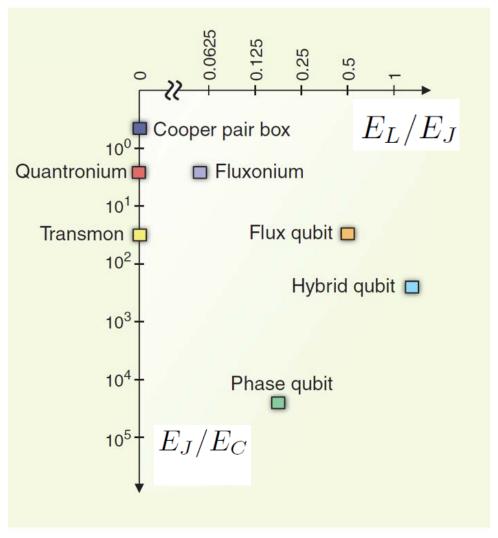
$$\frac{1}{T_2} = \frac{1}{2T_1} + \frac{1}{T_{\phi}}$$

Decoherence time Relaxation time Dephasing time



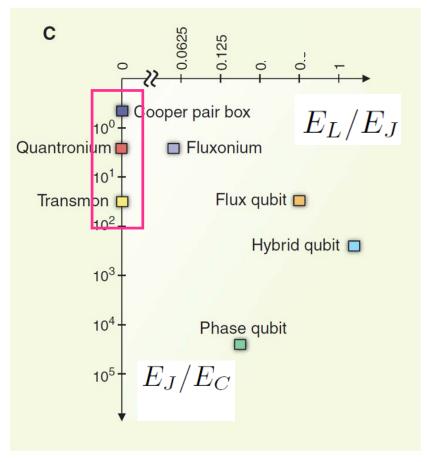
Dephasing

"Periodic table" of superconducting qubits

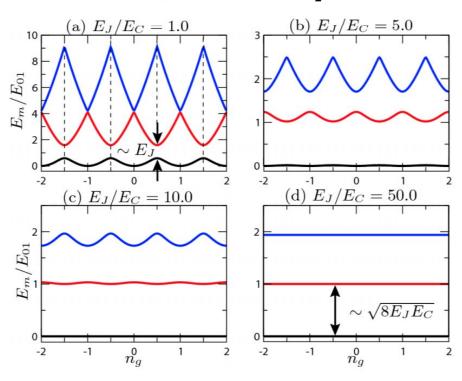


Devoret & Schoelkopf , Science **339**, 1169 (2013)

Control Sensitivity to Charge Noise: Ej/Ec



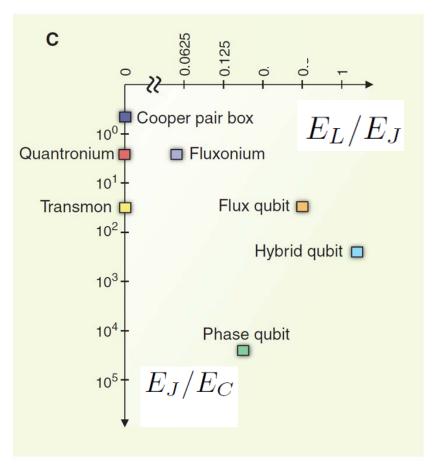
$$\widehat{H} = 4E_c(\widehat{n} - n_g)^2 - E_J \cos\widehat{\varphi} + \frac{1}{2}E_L(\widehat{\varphi} - \varphi_{ext})^2$$



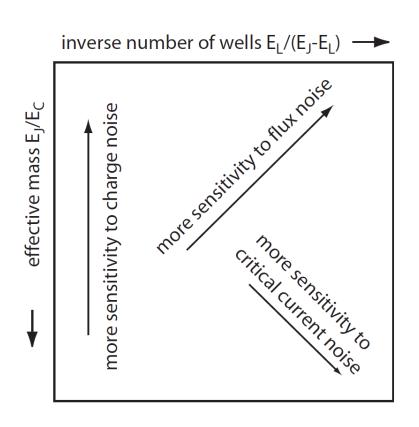
Koch et al., Phys. Rev. A 76, 042319

Devoret & Schoelkopf, Science 339, 1169 (2013)

Control Sensitivity to Various Noise Source

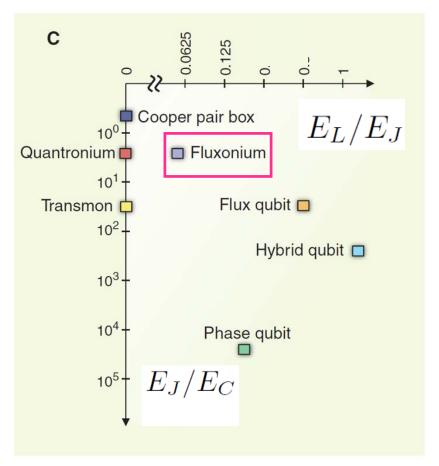


Devoret & Schoelkopf, Science **339**, 1169 (2013)

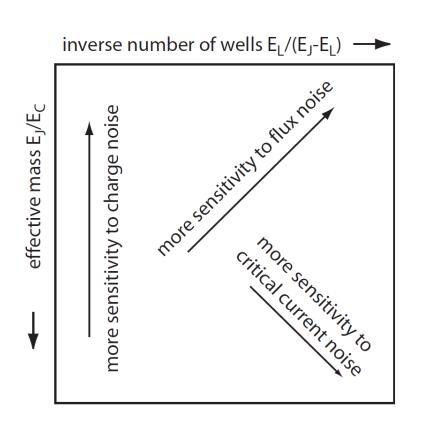


Vool & Devoret Int. J. Circ. Theor. Appl. 45, 897 (2017)

Control Sensitivity to Various Noise Source



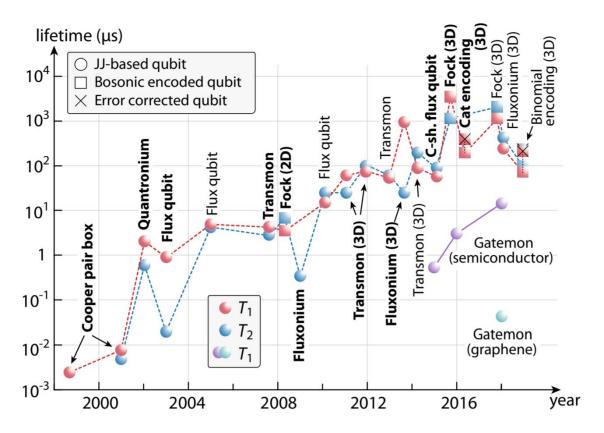
Devoret & Schoelkopf, Science **339**, 1169 (2013)



Vool & Devoret Int. J. Circ. Theor. Appl. 45, 897 (2017)

Key element: fluxonium

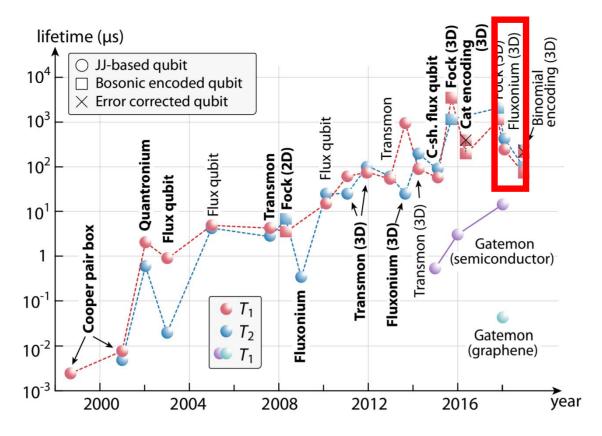
- Highest T1, and T2 of single superconducting qubit
- Anharmonicity can be larger than few GHz
- Very rich multi-level system



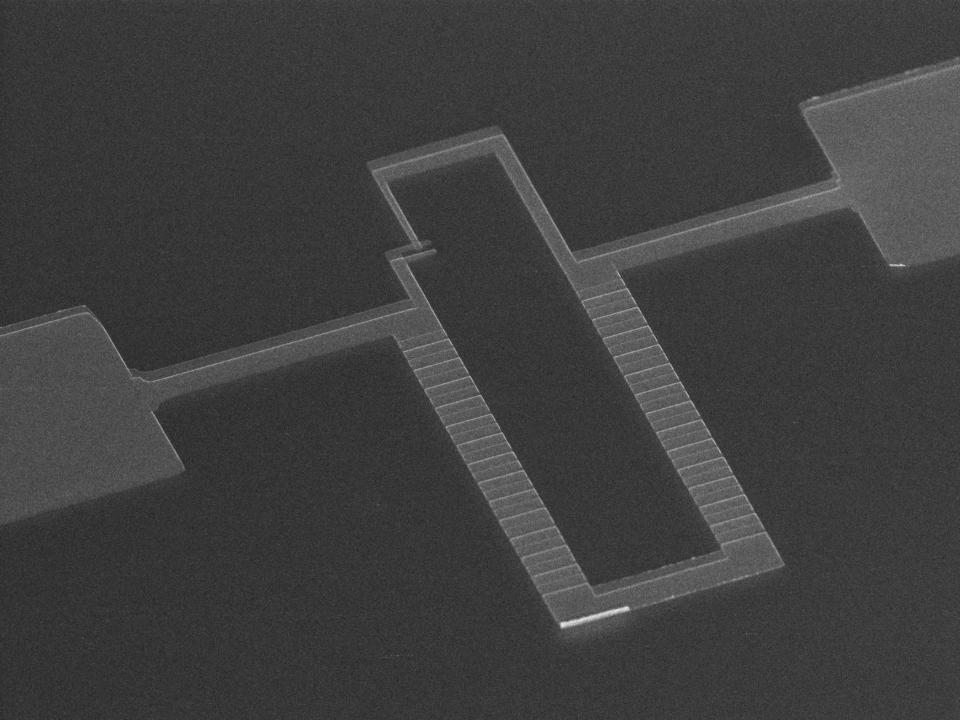
MIT group, Annual Review of Condensed Matter Physics 11, (2019)

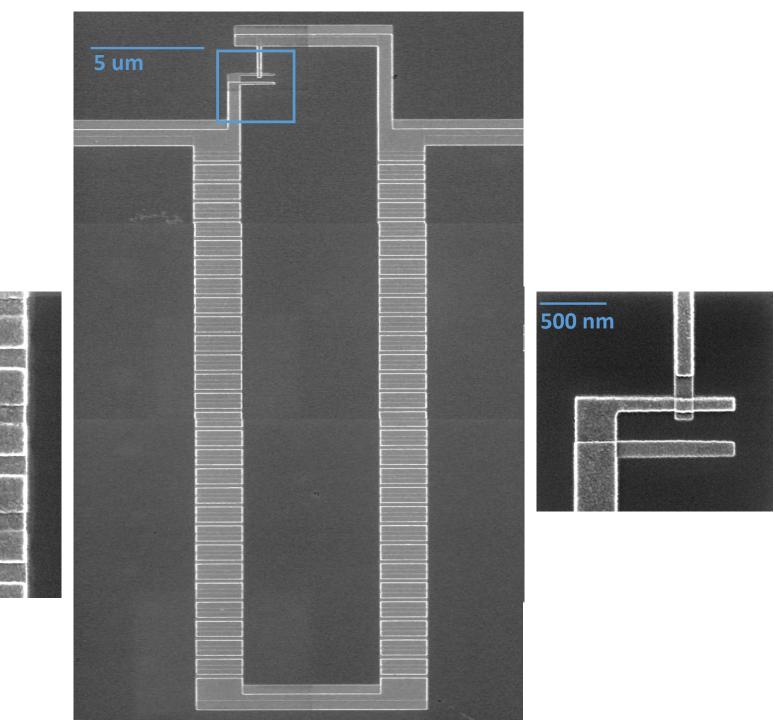
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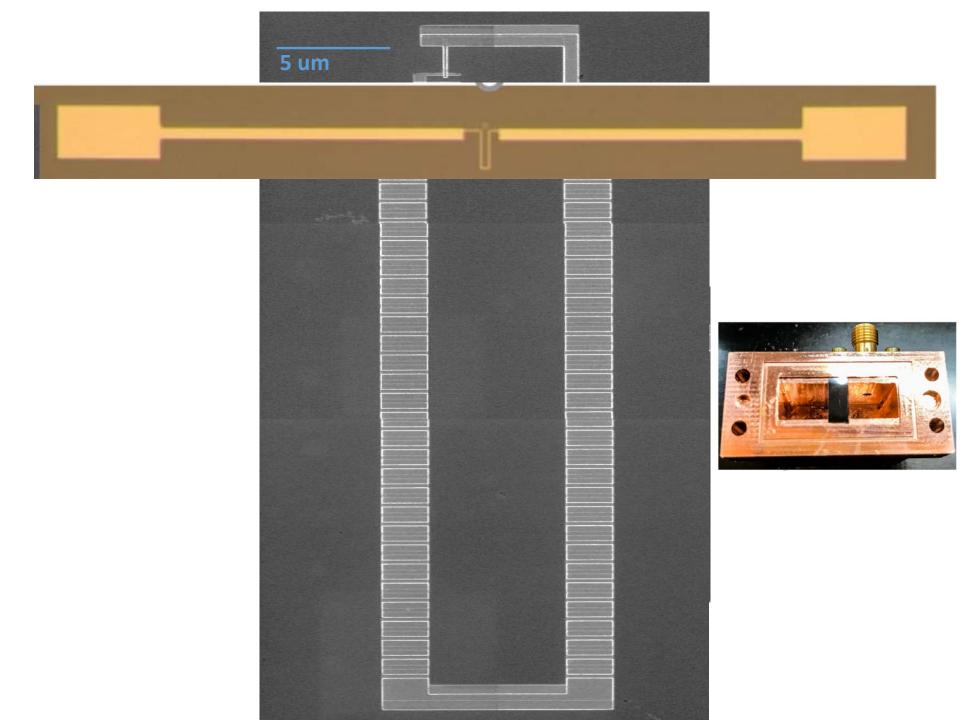


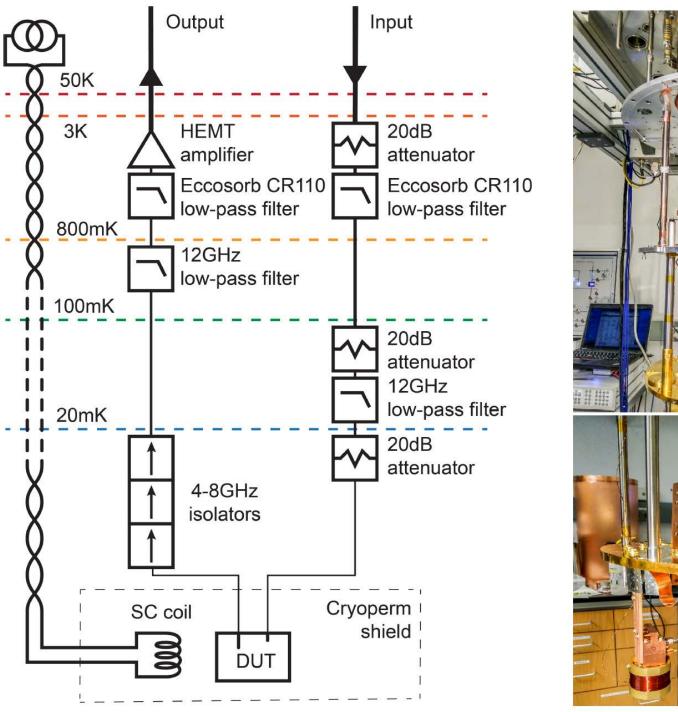
MIT group, Annual Review of Condensed Matter Physics 11, (2019)

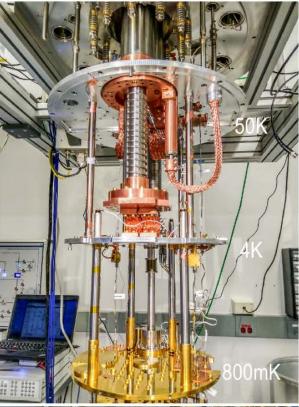


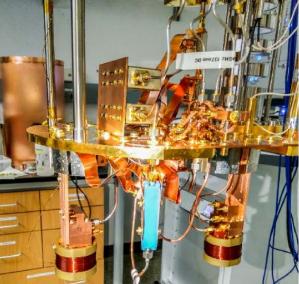


600nm

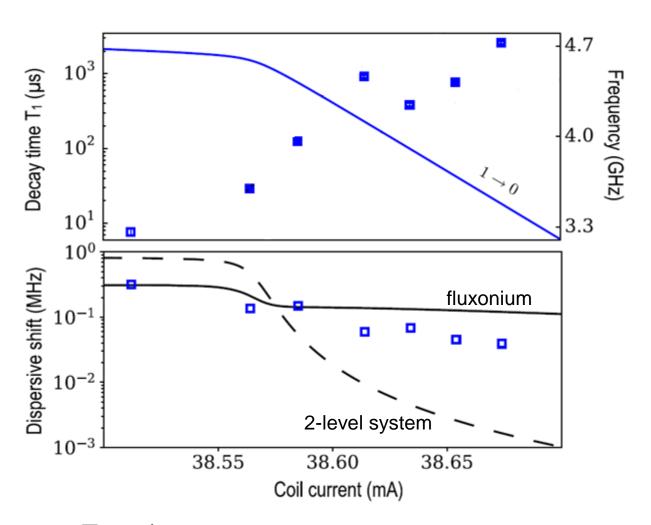








Demonstration world record T1



 $T_2 \approx 4~\mu {\rm s}$ due to flux noise But large L reduces sensitivity to flux noise

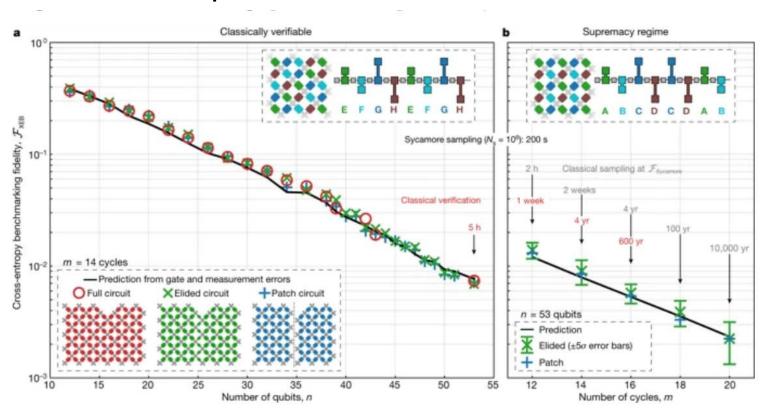
Reproducible world record T2 of superconducting qubit

| Qubit | E_J | E_C | E_L | N | T_1 | T_2 | $\omega_{01}/2\pi$ |
|-------|-------|-------|-------|-----|------------------|------------------|--------------------|
| | GHz | GHz | GHz | - | $\mu \mathrm{s}$ | $\mu \mathrm{s}$ | GHz |
| A | 3 | | | _ | • | | 0.78 |
| В | | | | _ | _ | | 0.32 |
| C | | | | | | | 0.48 |
| D | 2.2 | 0.83 | 0.52 | 196 | 70 | 90 | 0.56 |
| E | | | | | | | 0.83 |
| F | | | | | _ | | 0.17 |
| G | | | | | | | 0.55 |
| Н | 4.43 | 1 | 0.79 | 100 | 230 | 235 | 0.32 |

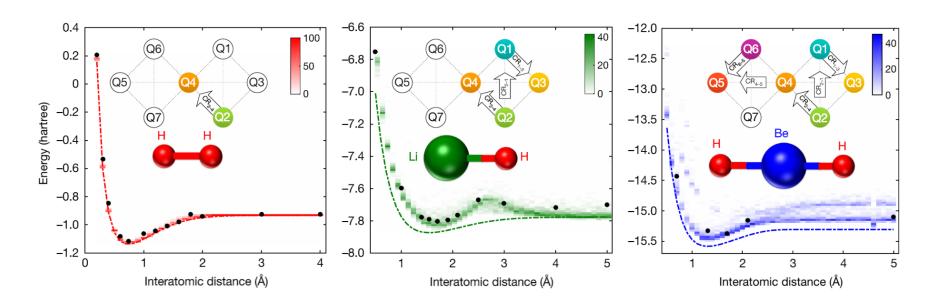
Nquyen, **Lin** et al., PRX 9, 041041(2019)

IBM Q 20 Tokyo: average T1= 78.34μs,T2=50.62μs

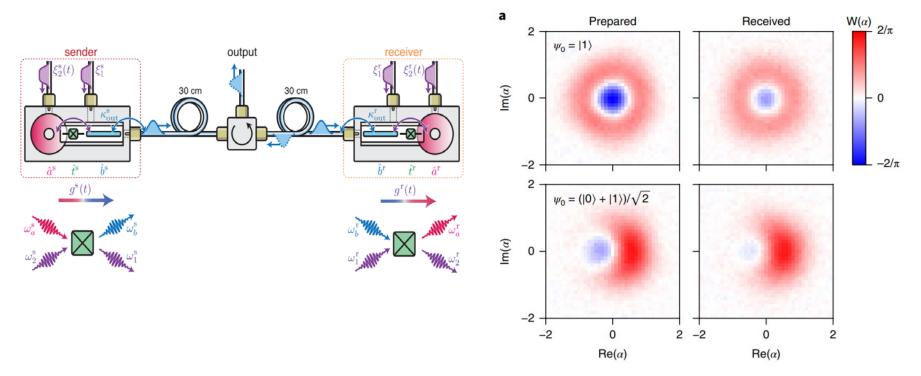
Quantum Computation



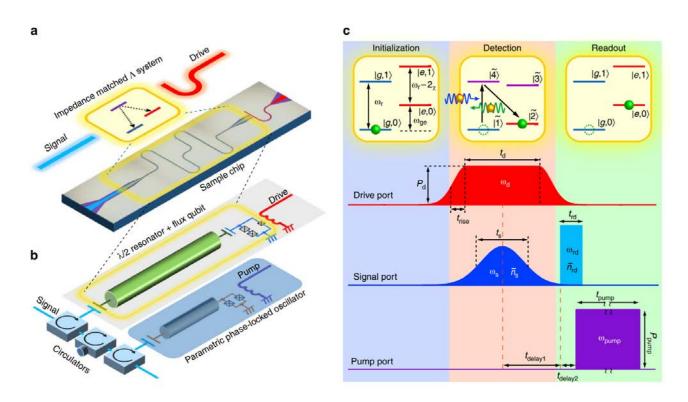
Quantum Simulation



Quantum Communication



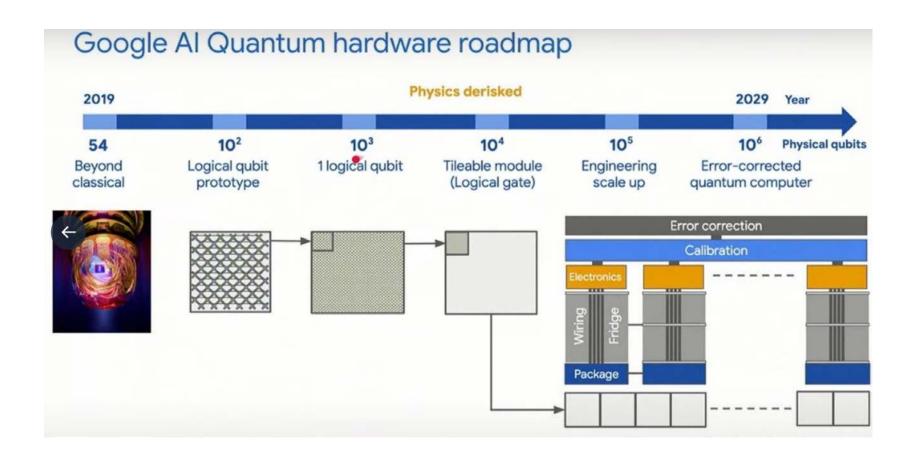
Quantum sensing and metrology



IBM roadmap for quantum computing

Scaling IBM Quantum technology IBM Q System One (Released) Next family of IBM Quantum systems (In development) 2019 and beyond 2020 2021 2022 2023 27 qubits 65 qubits 127 qubits 1,121 qubits Path to 1 million qubits 433 qubits Eagle and beyond Falcon Hummingbird Osprey Condor Large scale systems Scalable readout Optimized lattice Novel packaging and controls Miniaturization of components Integration Build new infrastructure. quantum error correction

Google's roadmap for quantum computing



Future important development

- Improvement and Scaling up
- Quantum Algorithm
- Quantum error correction and Fault tolerant quantum computers.
- Application for Noisy Intermediate-Scale Quantum (NISQ) machine.